

# Non-linearities beyond the OBC: Financial frictions and the elasticity of banking sector leverage

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- Gertler and Karadi (2011, 2013) became benchmark model for the study of macro-financial linkages
- It is frequently used to inform monetary policy-making
- However, the model exhibits a limited degree of pass-through from financial sector to the real economy under a reasonable set of parameters
- While the model illuminates financial sector dynamics, the moments of the financial variables are smaller than empirical evidence would suggest
- No substantial non-linearities beyond the occasionally binding leverage constraint

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We propose a model ingredient which provides a versatile tool to:

- 1 Generate a stronger pass-through from financial sector to the real economy
- 2 Achieve higher volatility of the banking sector leverage
- 3 Calibrate the model closer to the data without relying on non-standard model parameters or steady state calibrations
- 4 Introduce non-linearities beyond the occasionally binding leverage constraint
- 5 Have control over the degree of non-linearity of the model

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- Medium-scale New Keynesian model
- Standard household sector with habits in consumption
- Standard production sector with intermediate, final, and capital goods producers
- Government expenditures are financed through taxes and the issuance of government bonds
- Central bank sets nominal interest rate and conducts QE by purchasing government bonds

- Bank balance sheet

$$Q_t S_t + q_t B_{b,t} = N_t + D_t \quad (1)$$

- $S_t$ : corporate bonds with price  $Q_t$
  - $B_{b,t}$ : government bonds with price  $q_t$
  - $N_t$ : bank's net worth
  - $D_t$ : deposits
- Banks acquire deposits subject to an incentive constraint

$$V_t(N_t) \geq \Theta_t(X_t) \underbrace{(Q_t S_t + \Gamma q_t B_{b,t})}_{\text{Assets}} \quad (2)$$

- $V_t(N_t)$ : Franchise value of the bank
- $\Theta_t(X_t)$ : Diversion rate

- Diversion rate pins down the fraction of assets which are divertable
- In a GK model, the diversion rate is a constant  $\theta$
- Similar to Akinci et al. (2023), we introduce an endogenous diversion rate as a decreasing function of the share of safe assets

$$\Theta_t(X_t) = \theta \left( 1 - \frac{a}{b} X_t^b \right) \quad (3)$$

- $a$  and  $b$  are scaling parameters
- $X_t = \frac{\Gamma q_t B_{b,t}}{Q_t S_t + \Gamma q_t B_{b,t}}$  is the share of safe assets

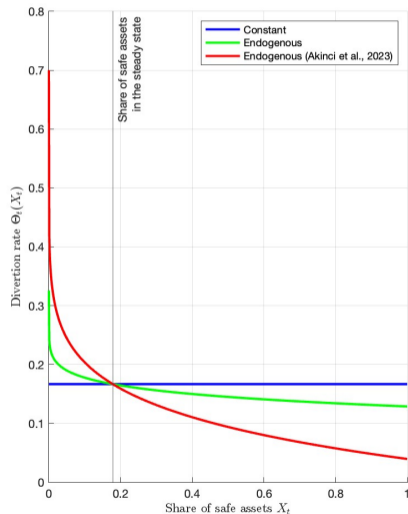
# Diversion Rate

- Intuition of an endogenous diversion rate
  - Reflects depositor ability to monitor banks' portfolios
  - If the riskiness of the portfolio increases, it becomes harder for households to monitor
  - Banker ability to divert funds increases

$$\frac{\partial \Theta_t(X_t)}{\partial X_t} < 0$$

- In order for the incentive constraint to be respected, the franchise value of bank has to increase with diminishing returns to riskiness

$$\frac{\partial^2 \Theta_t(X_t)}{\partial X_t^2} > 0$$



- Incentive constraint gives rise to an occasionally binding leverage constraint

$$\phi_t \leq \frac{\mu_{N,t}}{\Theta_t(X_t)(1 - \lambda_t)} \equiv \bar{\phi}_t \quad (4)$$

- $\phi_t = \frac{Q_t S_t + \Gamma q_t B_{b,t}}{N_t}$ : leverage ratio
  - $\bar{\phi}_t$ : maximum leverage
  - $\mu_{N,t}$ : Marginal value of banks' net worth
  - $\lambda_t$ : Lagrange multiplier on the incentive constraint
- Relationship between the lending spread and the leverage
    - Zero lending spread  $\rightarrow$  non-binding leverage constraint:  $\phi_t \leq \bar{\phi}_t$
    - Positive lending spread  $\rightarrow$  binding leverage constraint:  $\phi_t = \bar{\phi}_t$

# Set of modified equations

Diversion rate

$$\Theta_t(X_t) = \theta \left( 1 - \frac{a}{b} X_t^b \right) \quad (5)$$

Incentive constraint

$$\lambda_t = \max \left\{ 0, 1 - \frac{\mu_{N,t}}{\Theta_t(X_t) \phi_t} \right\} \quad (6)$$

Marginal value of lending

$$\mathbb{E}_t \Lambda_{t,t+1} \Omega_{t+1} [R_{k,t+1} - R_{t+1}] = \lambda_t \left[ \Theta_t(X_t) + \theta a X_t^b \right] \quad (7)$$

Marginal value of government bonds

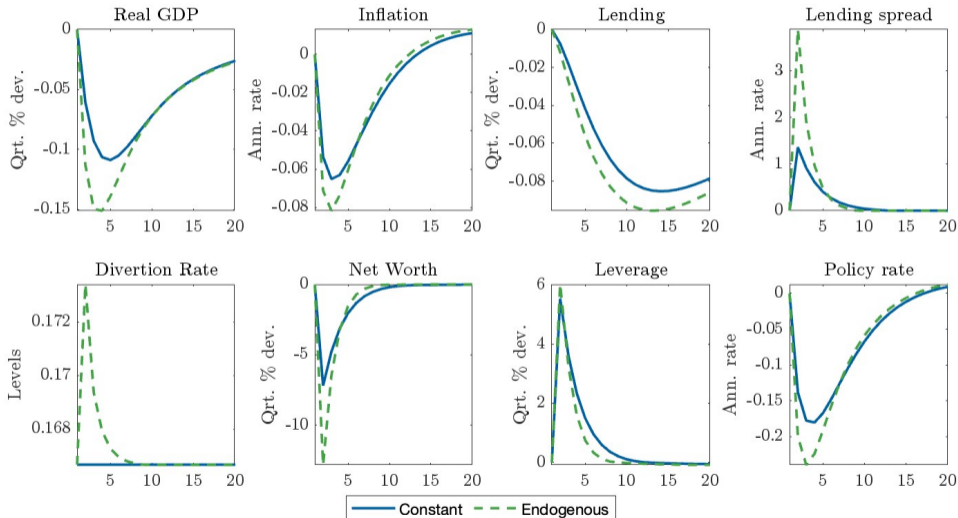
$$\mathbb{E}_t \Lambda_{t,t+1} \Omega_{t+1} [R_{b,t+1} - R_{t+1}] = \lambda_t \Gamma \left[ \Theta_t(X_t) + \theta a (1 - X_t) X_t^{b-1} \right] \quad (8)$$

For  $a = 0$ , the model reduces to a benchmark GK model.

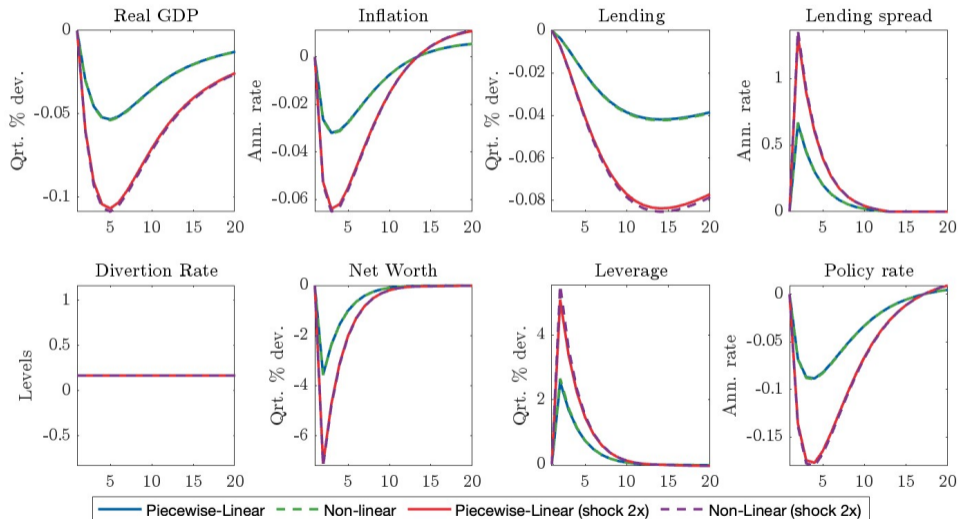
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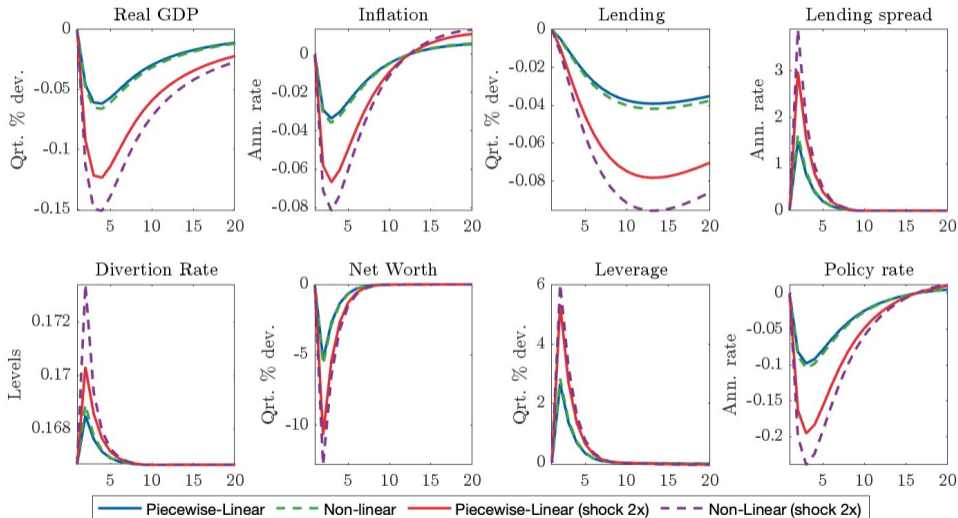
# Financial shock



# Non-linearities in the benchmark model ( $\alpha = 0$ )



# Non-linearities with endogenous diversion rate ( $\alpha = 0.075$ )



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Work in progress

- 1 Implement a simulation method that preserves non-linearities
- 2 Compare simulated moments with data and alternative models
- 3 Perform estimation of the model

- Akinci, O., Benigno, G., Del Negro, M., and Queralto, A. (2023). The Financial (In)Stability Real Interest Rate,  $r^{**}$ . *Federal Reserve Bank Staff Reports*.
- Gertler, M. and Karadi, P. (2011). A model of unconventional monetary policy. *Journal of Monetary Economics*, 58(1):17–34.
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